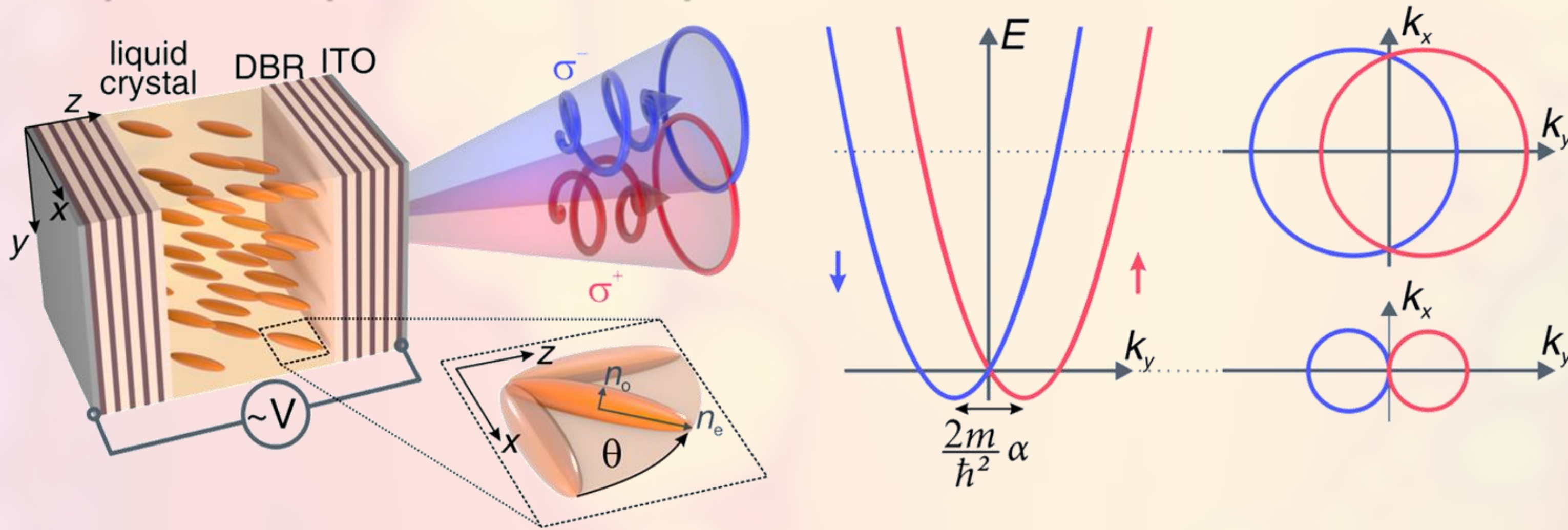


# Photonic Engineering of Spin-Orbit Synthetic Hamiltonians in Liquid Crystal Cavities

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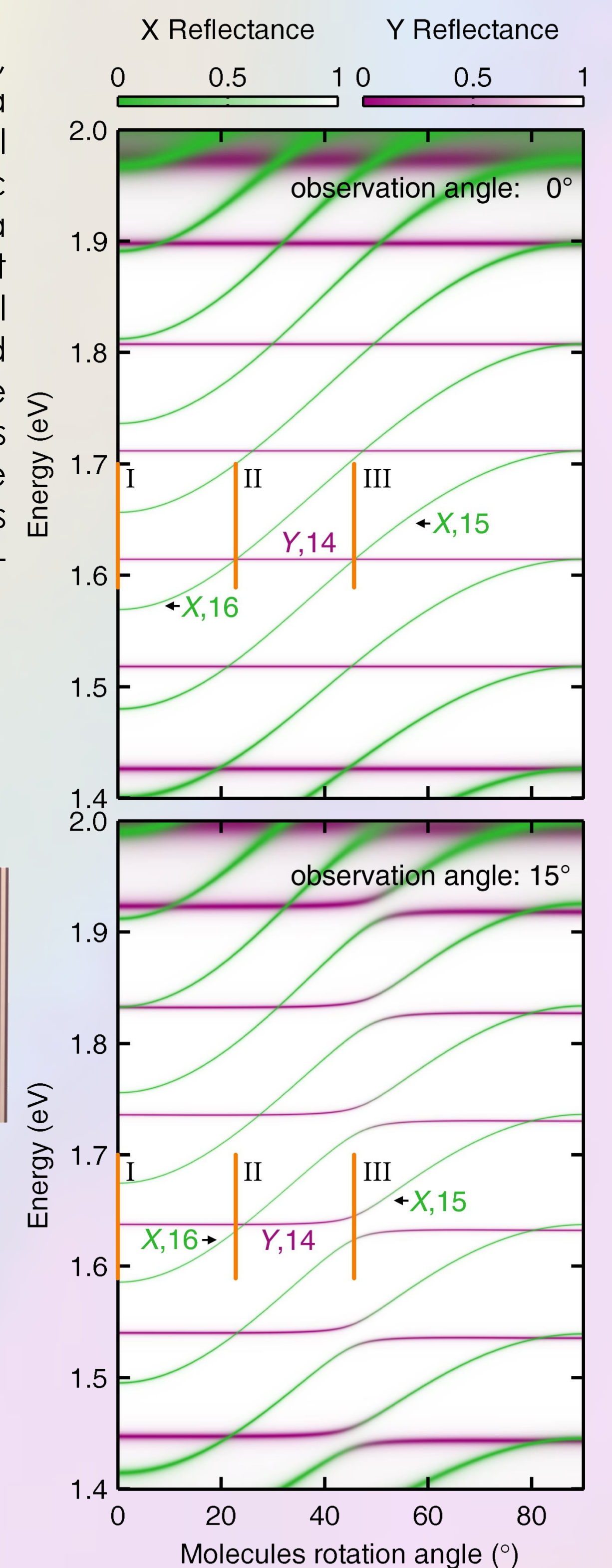
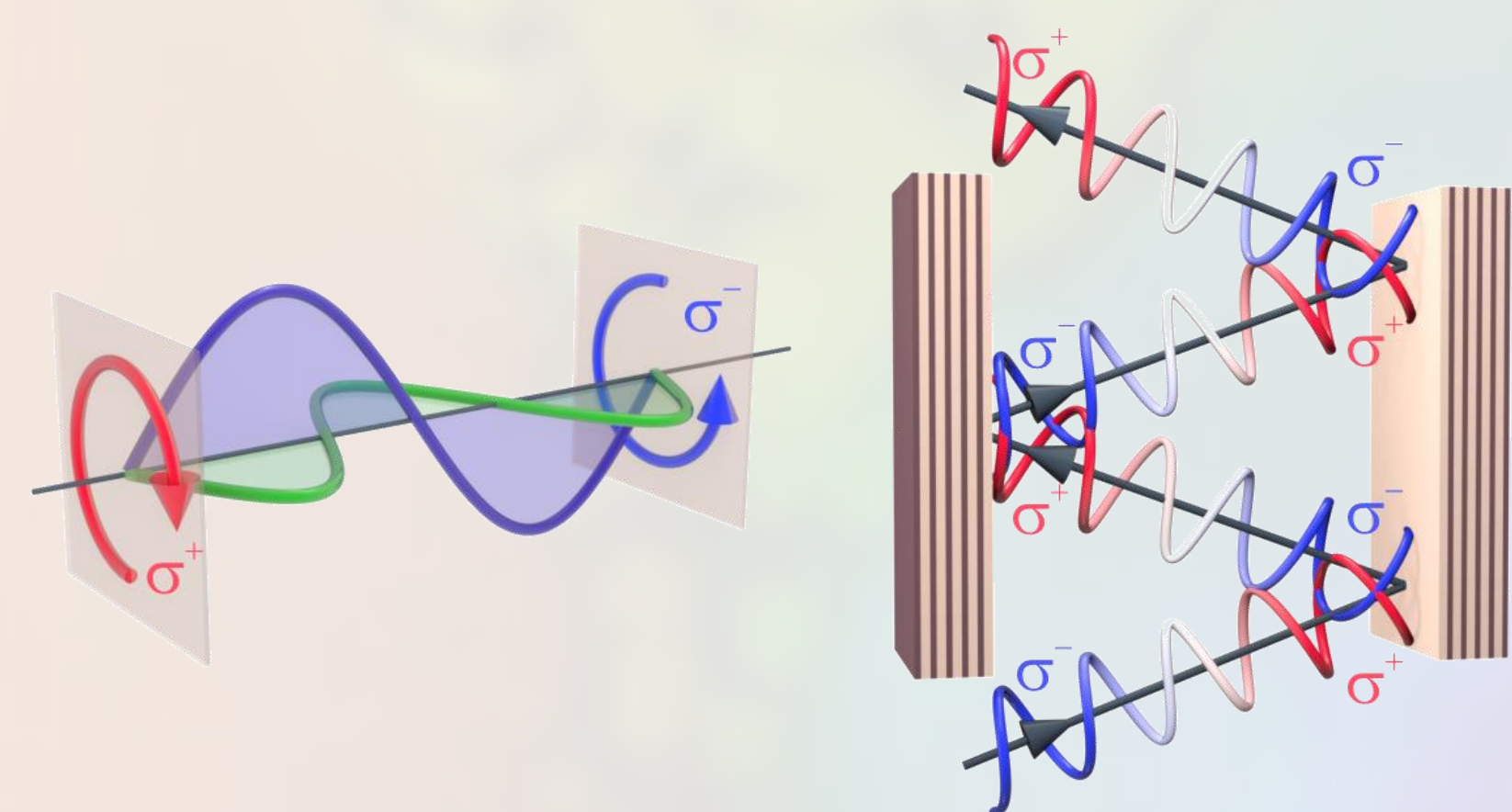
## Liquid crystal cavity for SOI



## Parity of the photonic modes

In this work we present a tunable, multimode microcavity consisting of a nematic liquid crystalline (LC) optical medium enclosed between two dielectric mirrors. Structure is surrounded by a transparent ITO electrodes to control the tilt angle of the LC molecules with external voltage, thus energy of the X-polarised cavity mode ( $E_X$ ). We show that for the energies of the X- and Y- polarised modes with the opposite parity mode number are close to degenerate a coupling term arises between them, which is equal to Rashba-Dresselhaus spin-orbit interaction:

$$\hat{H}_{R-D} = -2\alpha\hat{\sigma}_z k_y,$$



## Rashba – Dresselhaus Hamiltonian

Energy  $E$  of the cavity modes in a waveguide approximation are solutions of an eigenvalue problem. When the modes of opposite parity are close to degenerate, the equation reads:

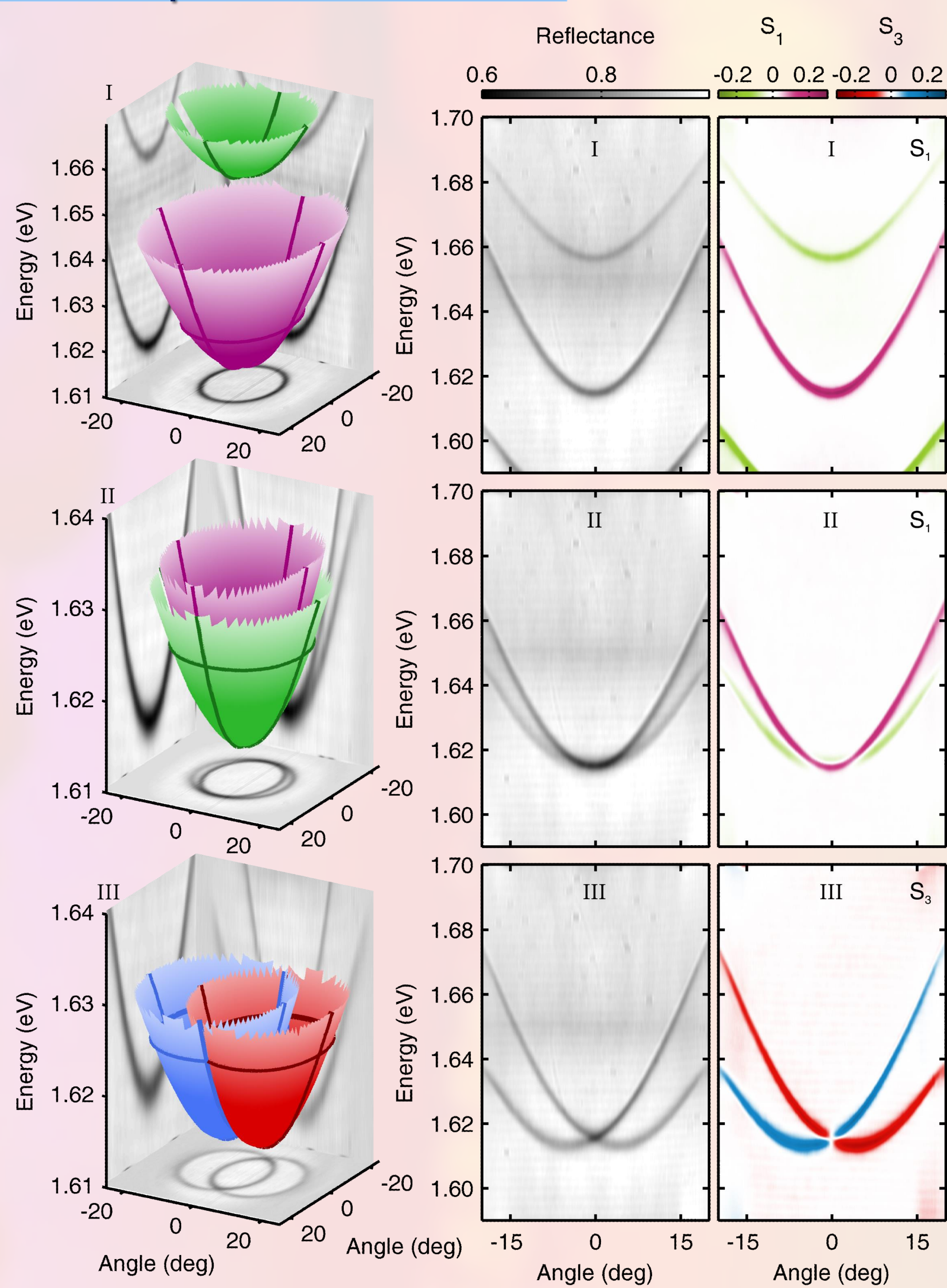
$$\left(\frac{\hbar^2 k_x^2}{2m_x} + \frac{\hbar^2 k_y^2}{2m_y}\right) \mathbf{F}' + (\delta_x k_x^2 + \delta_y k_y^2) \hat{\sigma}_z \mathbf{F}' - 2\alpha k_y \hat{\sigma}_y \mathbf{F}' + \frac{1}{2}(E_X - E_Y) \hat{\sigma}_z \mathbf{F}' = E \mathbf{F}',$$

When the modes of the same parity are degenerate, the equation leads to optical spin Hall effect Hamiltonian:

$$\left(\frac{\hbar^2 k_x^2}{2m_x} + \frac{\hbar^2 k_y^2}{2m_y}\right) \mathbf{F}' + \frac{\hbar^2}{4m_0'} \begin{pmatrix} \varepsilon_{xx} - \varepsilon_{yy} \\ \varepsilon_{zz} \varepsilon_{xx} \end{pmatrix} ((k_x^2 - k_y^2) \hat{\sigma}_z + 2k_x k_y \hat{\sigma}_x) \mathbf{F}' = E \mathbf{F}'$$

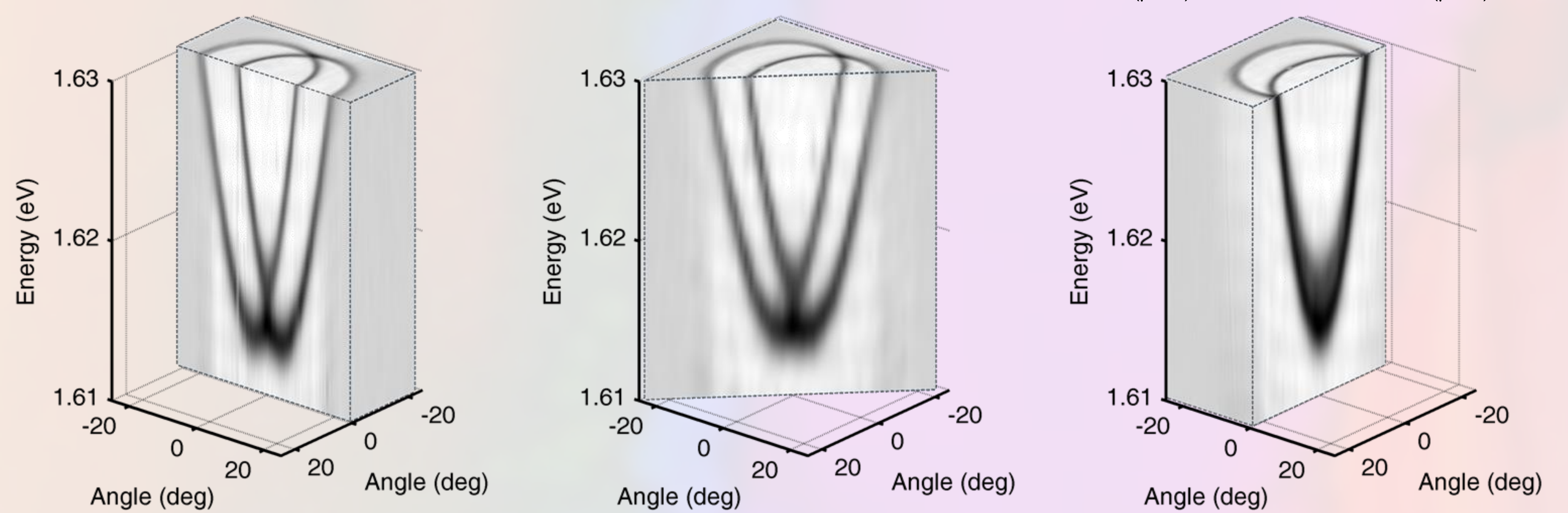
## Experiment

Hamiltonian describing experiment:  $\hat{H}_{exp} = \frac{\hbar^2 k_x^2}{2m_x} + \frac{\hbar^2 k_y^2}{2m_y} - 2\alpha \hat{\sigma}_z k_y + \frac{1}{2}(E_{X,l} - E_{Y,l'}) \hat{\sigma}_x$



k-space tomography in reflectance configuration at three specific voltages:

- I. 0.00 V: Cavity modes are parabolic, polarised linearly in the main axis of the LC molecules.
- II. 1.38 V: Parabolic cavity modes of the same parity (14 and 16) are degenerate at  $k = 0$ , but retain their initial linear polarizations.
- III. 2.48 V: Degenerate at  $k = 0$  cavity modes of opposite parity (14 and 15) reveal Rashba-Dresselhaus coupling between them. Dispersion relation consists of two, circularly polarised parabolas shifted in the reciprocal space.



## Spin-orbit synthetic Hamiltonians engineering

Coupling strength between the cavity modes of different parity increases linearly with the wavevector.

